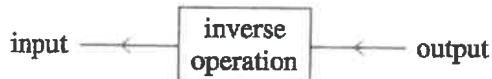


Inverse operations

- Using the *inverse* (or reverse) we can find the input for any machine, by using the output.



Operation	Inverse operation
+7	-7
-8	+8
×4	÷4
÷6	×6

- Example: Find the input.

$$? \rightarrow [+] 9 \rightarrow 20$$

Solution: Change arrows direction and use the inverse operation

$$? \leftarrow [-] 9 \leftarrow 20$$

$$? = 11 \text{ since } 20 - 9 = 11$$

Exercise 3

Find the input to these systems

- | | | | |
|------------------|----|-------------------|----|
| 1. → [+6] → 11 | 5 | 2. → [+4] → 13 | 9 |
| 3. → [-7] → 2 | 9 | 4. → [-12] → 24 | 36 |
| 5. → ×3 → 18 | 6 | 6. → ×5 → 45 | 9 |
| 7. → ÷8 → 4 | 32 | 8. → ÷7 → 8 | 56 |
| 9. → [+14] → 72 | 58 | 10. → [+11] → 29 | 18 |
| 11. → -13 → 31 | 44 | 12. → -72 → 27 | 99 |
| 13. → ×5 → 60 | 12 | 14. → ×9 → 72 | 8 |
| 15. ? → ÷4 → 8 | 32 | 16. → ÷6 → 7 | 42 |
| 17. → ×9 → 54 | 6 | 18. ? → ×8 → 56 | 7 |
| 19. → ÷7 → 7 | 49 | 20. → ÷3 → 27 | 81 |

Exercise 4

Find the input to these machines

1. $\emptyset \rightarrow [+8] \rightarrow [+6] \rightarrow 18$ 4
2. $\bullet \rightarrow [+2] \rightarrow [+5] \rightarrow 14$ 7
3. $\blacktriangleright \rightarrow [-5] \rightarrow [-8] \rightarrow 7$ 20
4. $\blacklozenge \rightarrow [-9] \rightarrow [-3] \rightarrow 6$ 18
5. $\forall \rightarrow [\times 3] \rightarrow [\times 3] \rightarrow 36$ 4
6. $\emptyset \rightarrow [\times 5] \rightarrow [\times 2] \rightarrow 70$ 7
7. $\circlearrowleft \rightarrow [\div 6] \rightarrow [\div 4] \rightarrow 4$ 96
8. $\blacktriangleleft \rightarrow [\div 2] \rightarrow [\div 5] \rightarrow 13$ 130
9. $\blacksquare \rightarrow [+7] \rightarrow [-11] \rightarrow 11$ 15
10. $\pi \rightarrow [+1] \rightarrow [-17] \rightarrow 1$ 17
11. $\blacktriangleright \rightarrow [+3] \rightarrow [\times 2] \rightarrow 16$ 5
12. $\blacktriangleleft \rightarrow [+3] \rightarrow [\times 4] \rightarrow 52$ 10
13. $\blacktriangleup \rightarrow [+4] \rightarrow [\div 5] \rightarrow 3$ 11
14. $\text{fish} \rightarrow [+7] \rightarrow [\div 9] \rightarrow 2$ 11
15. $\text{CD} \rightarrow [-2] \rightarrow [+17] \rightarrow 34$ 19
16. $\bullet \rightarrow [-16] \rightarrow [+61] \rightarrow 84$ 39
17. $\text{wavy lines} \rightarrow [-11] \rightarrow [\times 8] \rightarrow 40$ 16
18. $\$ \rightarrow [-8] \rightarrow [\times 7] \rightarrow 21$ 11
19. $\blacklozenge \rightarrow [-1] \rightarrow [\div 11] \rightarrow 4$ 45
20. $\blacksquare \rightarrow [-6] \rightarrow [\div 8] \rightarrow 32$ 262